

# Understanding Mechanics, Sadler and Thorning

## Exercise 2D, P31 (odd N<sup>o</sup>s only)

① given:  $u = 0 \text{ m/s} \downarrow$       want:  $V$   
 $s = 1.6 \text{ m} \downarrow$   
 $a = 9.8 \text{ m/s}^2 \downarrow$

$$\therefore v^2 = u^2 + 2as \Rightarrow v^2 = 0^2 + 2(1.6)(9.8) = 31.36$$

$$\text{so } v = 5.6 \text{ m/s}$$

③ given:  $u = 0 \text{ m/s} \downarrow$       want:  $s$   
 $a = 9.8 \text{ m/s}^2 \downarrow$   
 $v = 14 \text{ m/s} \downarrow$

$$\text{So } v^2 = u^2 + 2as \Rightarrow 14^2 = 0^2 + 2(9.8)s$$
$$\therefore s = 10 \text{ m}$$

⑤ given:  $u = +21 \text{ m/s} \uparrow$       want:  $s$   
 $a = -9.8 \text{ m/s}^2 \uparrow$   
 $t = 1, 2, 3 \text{ seconds}$

$$\text{So } s = ut + \frac{1}{2}at^2$$
$$\Rightarrow \text{at } t=1 : s = +21(1) + \frac{1}{2}(-9.8)(1)^2 = +16.1 \text{ m}$$

So Stone is 16.1 m above ground.

$$\text{at } t=2 : s = 21(2) + \frac{1}{2}(-9.8)(2)^2 = 22.4 \text{ m}$$

$$\text{at } t=3 : s = 21(3) + \frac{1}{2}(-9.8)(3)^2 = 18.9 \text{ m}$$

Extra: Note That between  $t = 2$  secs  $\rightarrow t = 3$  secs, The Stone has stopped rising  $\&$  is now falling. we can find The max height Reached by The Stone as follows:

given  $u = +21 \text{ m/s } \uparrow$  want:  $s$   
 $v = 0 \uparrow$   
 $a = -9.8 \text{ m/s}^2 \uparrow$

So  $v^2 = u^2 + 2as \Rightarrow 0^2 = 21^2 + 2(-9.8)s$   
 $\therefore s = 22.5 \text{ m.}$

(7) given:  $u = 21 \text{ m/s } \uparrow$  from A  
 $a = -9.8 \text{ m/s}^2 \uparrow$   
 $v = 0 \text{ m/s } \uparrow$  at its max height

want:  $t$

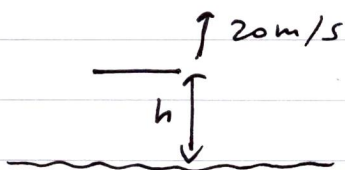
So  $v = u + at \Rightarrow 0 = 21 + (-9.8)t$   
 $\therefore t = \frac{21}{9.8} = 2.142857 = 2\frac{1}{7} \text{ seconds}$

But This is time to Reach max height, so total time to Reach max height  $\&$  come back is

$$2t = 2 \times 2.142857 = 4.285714 = 4\frac{2}{7} \text{ seconds}$$

(9) given:  $u = 20 \text{ m/s} \uparrow$       want:  $h$   
 $a = -9.8 \text{ m/s}^2 \uparrow$

Diag



First find max height. This is where  $v = 0 \text{ m/s}$ . So

$$v^2 = u^2 + 2as$$

$$\Rightarrow 0^2 = 20^2 + 2(-9.8)s$$

$$\Rightarrow s = 20.4082 \text{ m above}$$

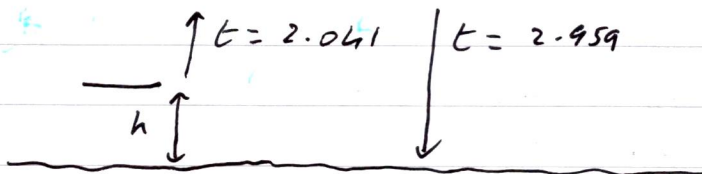
Now find total height above ground.

$$s = ut + \frac{1}{2}at^2 \Rightarrow s = 0 + \frac{1}{2}(9.8)t^2 \quad (*)$$

So we need to find time taken to get from max height to ground.

$$\therefore v = u + at \Rightarrow 0 = 20 - 9.8t \Rightarrow t = 2.041 \text{ sec to reach max height}$$

$$\therefore t = 5 - 2.041 = 2.959 \text{ sec to get from max height to ground}$$



$$\text{So now use } (*) : s = 0 + \frac{1}{2}(9.8)(2.959)^2 = 42.9082 \text{ m}$$

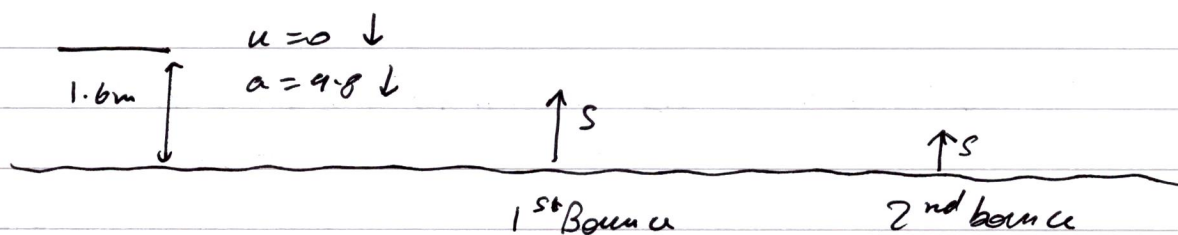
is total height above ground.

$$\text{Hence } h = \text{total height} - \text{height above } h$$

$$= 42.9082 - 20.4082 = 22.5 \text{ m}$$

(11)

given:  $u = 0 \text{ m/s} \downarrow$   
 $a = 9.8 \text{ m/s}^2 \downarrow$



Speed at impact is  $v$ : hence  $v^2 = u^2 + 2as$   
 $\Rightarrow v^2 = 0^2 + 2(9.8)(1.6) = 31.36$   
 $\therefore v = 5.6 \text{ m/s}$

Now  $u = \frac{1}{2}v \Rightarrow u = 2.8 \text{ m/s} \uparrow$   
 $\& a = -9.8 \text{ m/s}^2 \uparrow$   
 $\& v = 0$  at max height

So  $v^2 = u^2 + 2as \Rightarrow 0 = 2.8^2 + 2(-9.8)s$   
 $\therefore s = 0.4 \text{ m} = 40 \text{ cm}$  after 1<sup>st</sup> Bounce.

Now at top of 1<sup>st</sup> bounce:  $u = 0 \text{ m/s} \downarrow$   
 $a = +9.8 \text{ m/s}^2 \downarrow$   
 $s = 0.4 \text{ m}$   
Find  $v$

So  $v^2 = u^2 + 2as \Rightarrow v^2 = 0^2 + 2(9.8)(0.4) = 7.84$   
 $\therefore v = 2.8 \text{ m/s}$  as it hits the ground a second time.

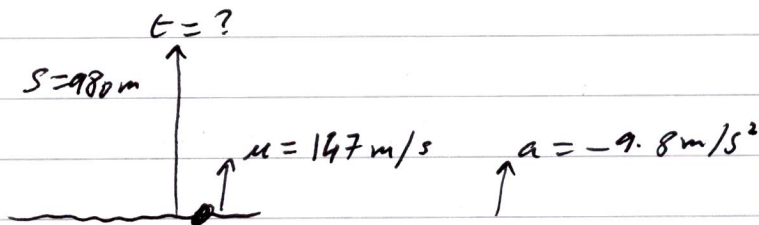
Now  $u = \frac{1}{2}v \Rightarrow u = 1.4 \text{ m/s} \uparrow$

So  $u = 1.4 \text{ m/s} \uparrow$   
 $a = -9.8 \text{ m/s}^2 \uparrow$   
 $\$ v = 0$  at top of bounce

$$\therefore v^2 = u^2 + 2as \Rightarrow 0 = (1.4)^2 + 2(-9.8)s$$

$$\therefore s = 0.1 \text{ m} = 10 \text{ cm}$$

(13)



given:  $u = 147 \text{ m/s}$       want:  $t$   
 $a = -9.8 \text{ m/s}^2$   
 $s = 980 \text{ m}$

$$\text{So } s = ut + \frac{1}{2}at^2 \Rightarrow 980 = 147t + \frac{1}{2}(-9.8)t^2$$

$$\Rightarrow 4.9t^2 - 147t + 980 = 0$$

$$\therefore t^2 - 30t + 200 = 0$$

$$\therefore (t - 10)(t - 20) = 0$$

$$\Rightarrow t = 10 \text{ sec or } 20 \text{ sec}$$

i.e. 10 sec to get upto 980m & 20 sec to come back down to 980m on its return journey.

(15)

$$\uparrow u_1 = 30 \text{ m/s} \uparrow ; a = 9.8 \text{ m/s}^2 \downarrow = -9.8 \text{ m/s}^2 \uparrow$$

$$\downarrow u_2 = 30 \text{ m/s} \downarrow ; a = 9.8 \text{ m/s}^2 \downarrow$$

<p>given: <math>u_1 = 30 \text{ m/s} \uparrow ; a = 9.8 \text{ m/s}^2 \downarrow</math>  <math>u_2 = 30 \text{ m/s} \downarrow ; t = 3</math></p>	want: $s$
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Now  $s = ut + \frac{1}{2} at^2 \Rightarrow$  For  $u_1$

$$s_1 = 30(3) + \frac{1}{2} (-9.8)(3)^2$$
$$= 45.9 \text{ m up}$$

For  $u_2$

$$s_2 = 30(3) + \frac{1}{2} (9.8)(3)^2$$
$$= 134.1 \text{ m down}$$

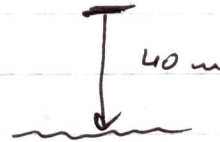
So distance between The two stones

$$s = s_1 + s_2 = 45.9 + 134.1 = 180 \text{ m}.$$

Ex 2D, P31 (even Nos only)

2

S	U	V	A	T
+40	0		+9.8	?



down as +ve

so  $S = ut + \frac{1}{2} at^2$

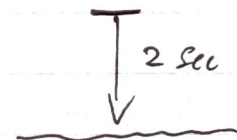
$\Rightarrow 40 = 0 + \frac{1}{2} (9.8) t^2$

$\Rightarrow t^2 = 8.163$

$\Rightarrow t = 2.86 \text{ sec}$   
 $= 2 \frac{6}{7} \text{ sec}$

4

S	U	V	A	T
?	+4		+9.8	2
✓		?		



down as +ve

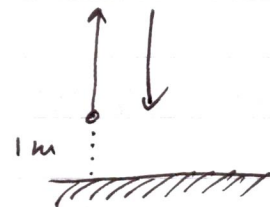
a)  $S = ut + \frac{1}{2} at^2$

$\Rightarrow S = (4)(2) + \frac{1}{2} (9.8) \cdot 2^2 = 27.6 \text{ m}$

b)  $V = u + at \Rightarrow v = 4 + (9.8)(2) = 23.6 \text{ m/s}$

6

S	U	V	A	T
?	28	0	-9.8	



up as +ve

a) No calculation involved:  $-28 \text{ m/s} = \text{velocity}$  so speed =  $28 \text{ m/s}$

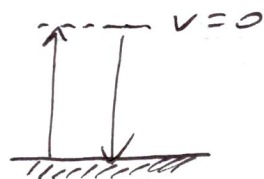
b)  $v = 0$  at highest point, so  $v^2 = u^2 + 2as$

$\Rightarrow 0 = 28^2 - 2(9.8)s$

$\Rightarrow s = 40$  From point of projection

8

S	U	V	A	T
?	14	0	-9.8	?



So  $S = ut + \frac{1}{2}at^2$

$\Rightarrow S = (14)$

Up as +ve

Does not work yet

So use  $v^2 = u^2 + 2as$

$\Rightarrow 0 = 14^2 + 2(-9.8)s \Rightarrow s = 10 \text{ m}$

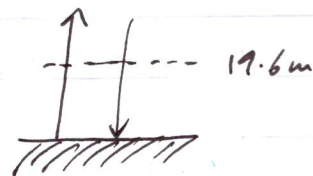
Then  $v = u + at \Rightarrow 0 = 14 - 9.8t \Rightarrow t = 1.43 \text{ sec}$

But this is to reach highest point. So total time =  $2 \times 1.43 = 2.86 \text{ sec}$

can not do S U V A T  
2014 9.8?  
since a changes direction

10

S	U	V	A	T
+19.6	+24.5		-9.8	?



So  $S = ut + \frac{1}{2}at^2$

$\Rightarrow 19.6 = 24.5t + \frac{1}{2}(-9.8)t^2$

Up as +ve

$\Rightarrow 4.9t^2 - 24.5t + 19.6 = 0$

$\Rightarrow t^2 - 5t + 4 = 0 \Rightarrow (t-1)(t-4) = 0$

(a) So first time  $t = 1 \text{ sec}$

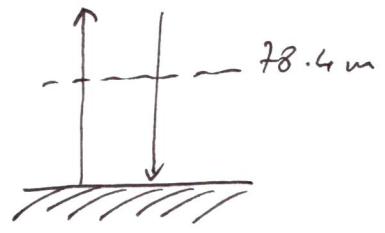
(b) 2<sup>nd</sup> time  $t = 4 \text{ sec}$

(c) "At least 19.6 m" means 19.6m or higher, so  $t = 4 - 1 = 3 \text{ sec}$ .



(12)

S	U	V	A	T
78.4	+49		-9.8	?



UP as +ve

So  $S = ut + \frac{1}{2} at^2$   
 $\Rightarrow 78.4 = 49t + \frac{1}{2} (-9.8) t^2$

$\Rightarrow 4.9t^2 - 49t + 78.4 = 0$   
 $\Rightarrow t^2 - 10t + 16 = 0$

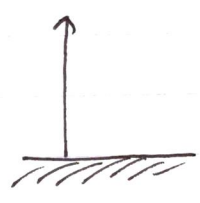
So  $(t-8)(t-2) = 0$

So object reaches 78.4 m after 2 secs & again after 8 secs.

$\therefore$  time spent at "at least 78.4 m" is  $t = 8 - 2 = 6$  secs. ✓

(14)

S	U	V	A	T
?	+14		-9.8	1
?	✓		✓	2



UP as +ve

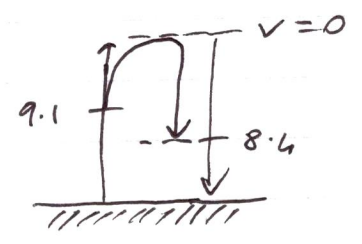
a)  $S = ut + \frac{1}{2} at^2$

$\Rightarrow S = 14(1) + \frac{1}{2} (-9.8) \cdot 1^2 = 9.1$  m

b)  $S = 14(2) + \frac{1}{2} (-9.8) \cdot 2^2 = 8.4$  m

c)

S	U	V	A	T
?	+14	0	-9.8	1



Max height:  $v^2 = u^2 + 2as$   
 $\Rightarrow 0 = 14^2 + 2(-9.8)s \Rightarrow s = 10$  m

So From 9.1 m to 10 m,  $S = 0.9$  m, & From 10 m to 8.4 m,  $S = 1.6$  m

$\Rightarrow$  Distance travelled in 2nd second is  $S = 0.9 + 1.6 = 2.5$  m ✓